Incorporating Multiple Technologies Into Teacher Education: A Case of Developing Preservice Teachers’ Understandings in Teaching Statistics With Technology

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The purpose of this paper is to present a multitechnology-enabled lesson used with secondary preservice mathematics teachers to develop their technological pedagogical statistical knowledge. This lesson engages preservice teachers in a statistics lesson aimed at developing their reasoning about the measurement units of data using TinkerPlots and then engages them in reasoning about students’ approaches to the task. A description of the lesson, preservice teachers’ approaches, and how they reasoned about sixth graders’ strategies are included. The authors further discuss the affordances of the specific technologies used in creating the learning opportunities for these preservice teachers and implications for teacher education.

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The importance of using technology in the preparation of preservice mathematics teachers (PSTs) has been at the forefront of national conversations in mathematics teaching and teacher preparation for over 15 years (e.g., Association of Mathematics Teacher Educators, 2015; Garofalo, Drier, Harper, & Timmerman, 2000; National Council of Teachers of Mathematics, 2000). Mathematics teacher educators (MTEs) are charged with promoting PSTs’ engagement with a variety of technological tools as well as mathematics-specific technologies that deepen understanding of mathematics and students’ thinking with technology.

Such engagement may require MTEs to make changes to their teaching goals to provide learning opportunities that better foster the development of PSTs’ technological pedagogical content knowledge (also referred to as technology, pedagogy, and content knowledge, or TPACK; Mishra & Koehler, 2006; Niess et al., 2009). Therefore, the purpose of this paper is to (a) present one approach for incorporating technology into a mathematics methods course that utilizes several types of technology into one lesson, (b) highlight affordances and limitations of different technological choices, and (c) discuss implications for teacher education.

Specifically, our approach situated MTEs as having to draw upon their own TPACK, where the specialized content was mathematics education, to create opportunities for PSTs to develop their TPACK, where the specialized content was a topic in secondary mathematics. To do so, MTEs have often used an approach to increase PSTs’ TPACK by engaging them in the tasks similar to those that they will be expected to use in their own classrooms, examining classroom videos, and students’ work to make sense of students’ reasoning about the task (e.g., Didis, Erbas, Cetinkaya, Cakiroglu, & Alacaci, 2016; Wilson, Lee, & Hollebrands, 2011). The task we chose to use is a data analysis activity we refer to as Mislabeled Variables (Appendix A), one that the instructor had previously taught to sixth-grade students (Lovett & Lee, 2016).

As students engaged in the Mislabeled Variables task, they investigated variable types (i.e., categorical and quantitative) and distributions generated from data gathered from a series of survey questions. Students used data collected from a class survey to make claims about which survey questions produced the data for each variable, where the variables are given letters names (e.g., $A$ and $B$) rather than descriptive names (e.g., gender or shoe size).

A data analysis task was chosen in response to the need to increase the preparation of PSTs to teach statistics, as reflected in the increased emphasis on statistics in recent years in the K-12 curriculum (National Council of Teachers of Mathematics, 2000; National Governors Association Center for Best Practice & Council of Chief State School Officers, 2010). Research has shown that many preservice secondary teachers do not possess the statistical knowledge needed to teach statistics effectively and often are not provided enough learning opportunities related to statistics learning and teaching in their mathematics methods courses (Lovett, 2016). In this context we chose to pose the Mislabeled Variables task to our PSTs.

The lesson was designed and enacted in an undergraduate mathematics education course for middle school and high school mathematics teachers taught by the first author at a large southeastern university. This lesson consisted of two parts: (a) PSTs engaged in the Mislabeled Variables task, and (b) PSTs watched and discussed a video case of sixth-grade students’ answers, reasoning, and misconceptions on the same task.
Video cases are a common tool used by MTEs and researchers to help PSTs reflect on their own knowledge and practice, and they allow PSTs opportunities to observe and understand professional practice and students’ mathematical reasoning (Grossman et al., 2009; Lampert & Ball, 1998; van Es & Sherin, 2002, 2008). Short clips that highlight important classroom moments are recommended because they can be viewed repeatedly to focus on important classroom moments (Borko, Jacobs, Eiteljorg, & Pittman, 2008; LeFevre, 2004).

We were unable to videotape the classroom when the task was enacted with sixth-grade students, so we chose to create a brief animated video to illustrate the classroom scenario that included samples of students’ work. Animations allow MTEs and researchers to recreate a real classroom environment without introducing cameras and microphones into the classroom. They are also useful when capturing high quality sound of what the teachers and students are saying is not possible (Chazan & Herbst, 2012).

**Literature Review**

Research exploring animations in mathematics teacher education is still in its infancy. The majority of the prior research conducted has examined the use of LessonSketch, an online environment that enables users to create representations of classroom scenarios (Herbst, Aaron, & Chieu, 2013). While conducting a professional development with in-service teachers, Chazan and Herbst (2012) found that participants were able to identify with the fictional teacher and that the animation did not inhibit participants’ discussion of the instruction depicted in the video. Teachers were also able to project their previous classroom experiences onto the characters in the animation so they could have a discussion about their experiences.

In another study, Herbst, Aaron, and Erickson (2013) asked preservice teachers to rate videos and animations on their genuineness. In addition, the researchers explored preservice teachers’ capacity to notice pedagogical and content knowledge features of the animations, asking them to reflect on alternate actions of the teacher while considering their previous experiences. The researchers found no significant differences in ratings in any of the measures except in genuineness, concluding that animations could be just as effective as video case examples in teacher education. In light of these findings, we had evidence that an animation of student engagement with the Mislabeled Variables task might provide PSTs with an authentic glimpse of student strategies.

**Framing the Task Design**

In the design of the lesson, we extended Lee and Hollebrands’ (2011) three aspects of teachers’ knowledge related to teaching statistics with technology to characterize four types of teachers’ knowledge: (a) statistical knowledge (SK), (b) technological statistical knowledge (TSK), (c) pedagogical statistical knowledge (PSK), and (d) technological pedagogical statistical knowledge (TPSK; Lee & Nickell, 2014).

Statistical knowledge is foundational for developing statistical knowledge for teaching and technological pedagogical statistical knowledge (Groth, 2013; Lee & Hollebrands, 2011). To assist in the development statistical knowledge, PSTs should engage with technology-enabled tasks that allow exploratory data analysis (EDA). To develop TSK, PSTs should engage in tasks with dynamic statistical software that encourages simultaneously development of statistical ideas and technological skills.
In terms of PSK, particular pedagogical decisions arise when teaching statistics that differ from other areas of mathematics, such as (a) planning for group projects and discussions about data, (b) supporting students in making statistical arguments based on appropriate evidence, and (c) considering the contexts used for teaching statistical ideas. Therefore, PSTs should learn to engage students in statistical investigations in a variety of contexts that require students to make decisions and arguments and consider how they respond to different conclusions among groups during discussions (Shaughnessy, 2007).

The ultimate goal in the preparation of PSTs to teach statistics with technology is to develop the specialized subset of knowledge representing TPSK. This type of complex knowledge is likely to develop with extended experiences with technology and considerations of the impact of such tools on the teaching and learning of statistics. MTEs are tasked with designing technology-enabled learning environments that develop aspects of PSTs' TPSK. The technologies chosen will impact what aspects of TPSK that PSTs have an opportunity to develop.

Madden (2011) suggested that tasks used with teachers can be provocative in the sense that they can excite and stimulate focused conversations and attention to statistics, context, and technology. Tasks can also be pedagogically provocative since they can stimulate a focus on pedagogical issues within statistics. Within SK, this study focused on engaging PSTs in statistical thinking through explorations of real data using TinkerPlots (Konold & Miller, 2011) and analyses of data to draw conclusions. In this way, the statistical knowledge that PSTs developed may have been interwoven with their technological statistical knowledge (TSK), which focused on using technology to explore and analyze data.

Within PSK, the Mislabeled Variables task focuses on providing PSTs with experiences with group work and supporting arguments with evidence that could be used as a foundation for planning their own lessons. Within TPSK, the goal is to provide PSTs with opportunities to reason about students' learning of statistical ideas with technology.

The Mislabeled Variables Task for Preservice Teachers

We identified learning objectives related to SK, TSK, PSK, and TPSK to guide our planning. The content objective (SK) was to increase PSTs' ability to reason about the context of data and measurement units; to engage with a multivariate data set with a dynamic statistical tool, TinkerPlots; and to make claims about reasonable contexts for different data distributions. In terms of PSK, objectives were to encourage PSTs to justify their reasoning with data-based evidence, to critique the reasoning of others, and to consider how to promote this type of reasoning and critique in students.

The TSK objective was for PSTs to learn how dynamic statistical software can support initial data exploration using dot plots, dynamic linking, and coordination of two or three variables. Lastly, for TPSK the objective was for PSTs to reason about students' statistical understandings and misunderstandings and approaches to the task while using a dynamic statistical software.

Engaging Preservice Teachers in the Task as Learners

It was important to engage PSTs in the Mislabeled Variables task first as learners (to develop SK and TSK) using the task as it was previously taught to sixth-grade students (Lovett & Lee, 2016). The Mislabeled Variables task was adapted from Garfield and Ben-Zvi's (2008) Variables on Backs, a task designed to assist introductory statistics students in developing an understanding that different statistical questions produce different types
of variables. The Variables on Backs task was enhanced through the use of TinkerPlots to explore survey questions, types of variables that questions produce, measurement units, and expected data values.

To begin the Mislabeled Variables task, PSTs completed a personal information survey as a Google Form containing 16 questions (e.g., “What time did you go to bed last night?”). Questions were chosen intentionally to produce different data types (e.g., whole numbers, decimals, and time values). Survey responses were gathered online and used to create a data set in TinkerPlots, in which 16 attribute names were labeled as A, B, C, and so forth, and randomized so as not to match the order of questions from the survey. See Appendix B for the survey questions and assignment of the corresponding letters. (The Mislabeled Variables task for teacher educators is also available as a resource in the Teaching Statistics Through Data Investigations MOOC-Ed, friday.institute/tsdi)

In class, PSTs were seated using a single laptop with access to a practice file and the class survey data in TinkerPlots. The instructor provided a quick tutorial on using TinkerPlots, since PSTs had no prior experience with the software. This tutorial included an introduction to the cards, an explanation of how TinkerPlots uses colors to represent quantitative and categorical variables, and step-by-step instructions for creating a plot, separating data, and stacking data. An identical tutorial was provided to sixth graders. Next, each pair of PSTs was assigned data from two attributes and asked to make a conjecture about survey questions that most likely generated the data. Attributes were assigned so that each PST pair reasoned about different types of data (e.g., whole numbers, decimals, and time values). The attributes of C, F, I, J, O, and P were assigned to at least two groups, since these data were featured in the animation to be used during the second portion of the lesson.

Following small group work, the instructor modeled Common Core Mathematical Practice 3, “Construct viable arguments and critique the reasoning of others” (National Governors Association Center for Best Practice & Council of Chief State School Officers, 2010) by engaging PSTs in a class discussion. PSTs presented claims and evidence about the match between the attribute and the source of the data to their peers and critiqued the reasoning of others. The instructor purposefully chose PSTs to present their group’s approach, encouraging PSTs to examine specific attributes and demonstrate different ways of reasoning about the task.

**Pedagogical Focus of the Lesson**

Following their engagement in the task, the PSTs watched a video case of sixth-grade students’ answers, reasoning, and misconceptions – specifically, a 3-minute animation created with GoAnimate to depict examples of how sixth grade students reasoned when they had completed the task (see Video 1). This animation provided the instructor with the opportunity to use authentic artifacts to engage PSTs in sense-making activities with student work (as in, e.g., Didis et al., 2016; Wilson et al., 2011).

The instructor showed the animation once to help PSTs understand the content of the animation. Then, the instructor directed PSTs to focus on claims provided by the sixth graders and how these claims were similar or different to those made by PSTs. The instructor showed the animation a third time and directed the PSTs to focus on ways in which students reasoned about the data and engaged with TinkerPlots. The PSTs compared and contrasted this engagement with their own use of the software.
Classroom Implementation: A Focus on Sequencing the Class Discussion

During small group work on the first part of the lesson when PSTs were engaged as learners with the Mislabeled Variables task, the instructor strategically identified PSTs to present their work during the class discussion. The following sequence was purposefully chosen so PSTs’ reasoning and approaches would increase in sophistication throughout the class discussion and align with the animation of the sixth graders’ reasoning discussed in the second part of the lesson.

Range of Values

The first two groups supported their claims through a discussion of the range of the data values. Amy and Ed claimed that letter E represented “What month were you born in?” and justified this hypothesis by noting, “The values went from 2 to 12, and 12 is the maximum.” Amy said that she was born in December, so she felt that this was a reasonable claim.

The class did not find this evidence wholly convincing. To verify the claim, Amy polled the class to determine if anyone was born in January or August. Since there were no data values for either of those months and since no one was born in January or August, the class was convinced that the claim was true.

Reagan and Molly used a similar technique to provide evidence for letter A. They claimed A was the total number of letters in the first and last name. They looked up everyone’s name on our course management system and counted the letters. Noting that one classmate had a total of eight letters in their name and another had 17 and that these values were the same as the minimum and maximum data values for letter A, the class was convinced that this claim was true.

Multiple Representations
Next, PSTs looked for questions on the survey that might match attribute $F$. We chose Morris’ group to present first since their supporting evidence was not conclusive. Specifically, they claimed that data from $F$ was generated from the survey question, “What is your gender?” Morris noted that the data consisted of ones and zeros and, thus, had to correspond to one of two questions that could produce this type of data. He supported his argument with evidence that there were 11 females in class, which were represented as zeros. Another student pointed out that attribute $C$ also had data containing 11 zeros and 10 ones. The instructor asked Morris if it bothered him that he did not know which attribute represented $F$ and which represented $C$. Although Morris was not bothered by this circumstance, other PSTs were.

The instructor then asked Kadeem’s group to present work utilizing multiple representations to support their claims. Kadeem suggested examining shoe size because men typically have larger shoe sizes than women and, as such, this would help identify gender. Kadeem believed attribute $J$ represented shoe size because of the range of the data. Another student in class supported Kadeem’s claim by pointing out the data values of $J$ consisted entirely of whole or half values and that only two questions of the survey were capable of producing half values.

At this point, Cam, Kadeem’s partner, went to the board and demonstrated how he used technology to coordinate his reasoning among the attributes $C$, $F$, and $J$ (Figure 1). Cam knew that there was a male student in the class with a size 14 shoe, so he displayed three graphs, $J$ vs. $C$, $J$ vs. $F$, and $J$. He highlighted the data point of 14 in $J$ and showed where that point appeared in the other two graphs (Figure 2). With this evidence, the class agreed that attribute $C$ represented gender, and $F$ represented wearing glasses.

![Figure 1. PST sharing his explanation of multiple attributes and use of multiple representations.](caption)

![Figure 2. Cam’s graphs dynamically linking representations.](caption)
Identifying Their Own Card

To conclude the class discussion, the instructor asked Joelle and Bethany to share their approach to determining letter $O$. Their claim was that $O$ was generated by the question “What time did you go to bed last night?” Joelle and Bethany did not create a graph as their evidence, instead presenting Bethany’s card, card 12.

The instructor asked the PSTs to justify how they knew it was Bethany’s card. Pointing to the values on the card, Bethany noted, “I have 13 letters in my first and last name. I have 2 siblings, 8 pets, and a 9.5 shoe size. I woke up at 10 on Saturday, and I have seven letters in my first name.” The class found this argument convincing.

Five of the seven groups used this approach as evidence for one of the attributes they were assigned. However, the instructor was still skeptical and asked Bethany how she knew that the unit associated with 10 was a measure of time. Joelle flipped to a different card and showed that $O$ had values written in an hour:minute format. Bethany’s value was not written in that form, and the PSTs decided that one card did not provide sufficient evidence to identify all the attributes.

Discussion of the Animation

After watching the animation, the instructor asked PSTs to evaluate answers and claims made by sixth graders. As a class, PSTs claimed that the students incorrectly identified $J$ as hours slept. The PSTs had already presented evidence and decided that $J$ corresponded to shoe size; therefore, they were convinced that the sixth graders’ reasoning was flawed. PSTs agreed with the other answers presented by the sixth graders.

After showing the animation a third time, the instructor asked the PSTs to consider the strategies sixth graders used to reason about the attributes. The instructor asked PSTs first to identify similarities between their approaches and those of the sixth graders. Several PSTs noted that sixth graders used strategies similar to their own. For instance, both groups considered the range of values and type of data while locating their own cards in the data set.

Morris pointed out that the students used the graphs of $C$ and $F$ simultaneously to compare attributes $C$ and $F$. As a class, the PSTs noted that both they and the students used multiple representations, although students did not use the technology to the same degree of sophistication.

When considering the differences between themselves and sixth graders, the PSTs pointed out immediately that the first pair of students formed an opinion but did not support their claim with evidence. PSTs also recognized that sixth graders reasoned in the aggregate, considering the measures of center to make a claim – an approach that none of the PSTs employed. PSTs were surprised that sixth graders had reasoned in a way that they had not.

Developing TPSK

Students’ reasoning and approaches to the Mislabeled Variables task fostered PSTs further development of SK, TSK, and PSK. For instance, PSTs employed different ways of reasoning, consistent with Konold, Higgins, Russell, and Khalil’s (2015) four different perspectives on data: data as a pointer, case-value, classifier, and aggregate. In drawing conclusions about the context of the data, PSTs utilized a variety of approaches, including
case-value and classifier. However, PSTs also used a different type of reasoning – the type of number (e.g., rational or whole number) – to reason about how such a number would make sense as a measurement of the context of a source of data. This perspective of reasoning about data as measurement was identified by Lovett and Lee (2016) in their study of sixth graders’ reasoning with the same task.

With no prior experience using TinkerPlots, PSTs were able to develop aspects of TSK as they discovered how to create and link multiple representations, using them to support their work and arguments. Related to TPSK, the PSTs demonstrated evidence that, while engaged in discussing the animated representation of students’ work on the task, they could reason about claims students presented while critiquing the students’ reasoning. PSTs recognized that students took different approaches than they did to solve the task, identified which approaches were common among students, and reasoned about different ways that students utilized or did not use different features in TinkerPlots.

**Affordances and Limitations of Technologies Used**

The instructor made a purposeful decision to include five technologies for PSTs in this lesson: (a) Google Forms, (b) TinkerPlots, (c) shared laptops, (d) projector and large display, and (e) a GoAnimate animation. As we considered the design and implementation of these five technologies, different affordances and constraints emerged with respect to PSTs’ growth and development of TPSK. We organize affordances and limitations for each technology in the following paragraphs.

**Google Form**

To plan and implement the task, it was most efficient for survey data to be collected prior to class time. To collect these data, we had PSTs complete the 16-question personal information survey using an online Google Form. Their answers populated a spreadsheet that was used to assign letters representing the attribute for each question and to sort data by alphabetical order by letter attributes. The spreadsheet was also used to import data into TinkerPlots.

A constraint of using a Google Form to collect data was that the data had to be cleaned prior to assigning letters for each attribute. Since the survey questions were posed as “short answers” in a Google Form, PSTs entered their answers in a variety of formats. For instance, PSTs often added units to their answer (e.g., a.m./p.m., hours, or men’s/women’s) and did not follow directions, for instance, reporting the exact time instead of rounding to the nearest half hour or using the name of the month instead of the corresponding number. Even though cleaning the data took time, it was preferable to the instructor entering data manually. Furthermore, the Google Form enabled the instructor to model online data collection practices for PSTs.

**TinkerPlots**

Incorporating TinkerPlots in the task enabled PSTs to analyze the entire data set with drag-and-drop data visualization tools, providing a more open investigation of all attributes from multiple perspectives. For instance, TinkerPlots allowed for quick construction of graphical representations, not only of the attributes a pair was assigned, but also other attributes PSTs wanted to explore. Such approaches are difficult, if not impossible, without dynamic statistical software. Because of the ease and speed that PSTs were able to construct graphical representations, they were able to spend the majority of the task reasoning and drawing conclusions about the data. While reasoning about the data and context, PSTs
were able to view multiple representations simultaneously and dynamically link representations of different attributes to make claims about the source of various data they were provided.

A limitation of incorporating TinkerPlots into the task was that PSTs were not able to fully utilize the capabilities for analyzing the data, since this was their first exposure to the software. However, this experience mirrored the experience of sixth graders. Even though it is identified as a limitation of the software, PSTs could easily navigate the basics of data visualization with different representations and did not need advanced features of TinkerPlots to engage with the Mislabeled Variables task.

**Shared Laptops and Projecting a Display**

Having pairs of PSTs share a laptop facilitated conversations around the data and encouraged PSTs to verbalize their reasoning to each other, illustrating to PSTs the usefulness of shared laptops for encouraging communication and collaboration. Similarly, PSTs used the classroom computer and projector to facilitate class discussion. Moreover, they used the class computer to recreate graphs as they taught their peers new skills. Such an approach demonstrated to PSTs how technology could be used in their own lessons to support sharing, discussions, and small group work.

**GoAnimate**

GoAnimate animation provided PSTs with an opportunity to examine authentic reasoning strategies of sixth-grade students. The animation enabled the instructor to recreate discussions from a sixth-grade classroom that were not video recorded. Moreover, the animation provided PSTs with access to real student work and reasoning. The actual sixth-grade class discussion took approximately 45 minutes. The most salient aspects of this interaction was choreographed and rendered as a 3-minute animation. The creation of this animation provided the instructor with an opportunity to more carefully consider ways in which PSTs may reason with the task.

Moreover, the animation production helped the instructor orchestrate the class discussion among PSTs to include attributes similar to those highlighted in the sixth-grade discussion. The brevity of the animation made it possible for PSTs to watch the video several times, comparing their own answers and approaches with those of the students in a manner supported by previous research (LeFevre, 2004).

A possible constraint of the GoAnimate animation is that it features characters with unusual appearances and voices, a possible source of distraction. Anticipating the animation could be disruptive, the instructor acclimated the PSTs to the animation during an initial viewing, showing the animation a second time while asking PSTs to focus on the answers and reasoning of the students. Furthermore, the animation does not feature real students; PSTs may prefer video of actual children to animated characters. However, the affordances and the amount of class time saved by using an animation seemed to outweigh these constraints.

**Implications for Teacher Education**

The work of MTEs requires the design of lessons covering topics that are often difficult to teach and learn, such as statistics, while incorporating technology to develop teachers’ TPACK (Association of Mathematics Teacher Educators, 2015). In the *Statistical Education of Teachers* report, Franklin et al. (2015) presented recommendations for
mathematics education programs to develop statistical knowledge and pedagogical statistical knowledge among their PSTs. These recommendations included engaging PSTs with real-world data sets through statistical investigation, developing knowledge of dynamic statistical software as a learner and as a teacher, analyzing student misconceptions, engaging in appropriate teaching strategies, and developing strategies for assessing students’ statistical knowledge.

With the limited amount of time that many teacher preparation programs have to devote to mathematics methods courses, it is worthwhile for MTEs to consider carefully which topics and which technologies should be targeted — namely those that have the greatest impact in the development of PSTs’ TPSK. The Mislabeled Variables task provides guidance to others confronted with challenging design decisions for creating technology-enabled learning environments.

Incorporating numerous different technologies into one task in a methods course can be time consuming, requiring considerable planning. The technologies highlighted in this lesson offered many affordances. Indeed, the data analysis task chosen, the easy-to-use capabilities of TinkerPlots for graphing, and the use of the animated video of students’ approaches all provided provocative opportunities aligned with Madden’s (2011) task framework. In particular, the use of the MTE-created animated video of students’ work on the task seemed to prove pedagogically provocative for enhancing PSTs’ PSK and TPSK.

Although Herbst et al. (2013) found that animations have the same impact on preservice teachers’ ability to reason about content and pedagogy as do video clips, more research is needed on how animations can be used in mathematics methods courses as an alternative to videos of actual classrooms, how different animation software provide different affordances or constraints for PSTs’ reasoning, and how these animations impact PSTs’ abilities to reason about students’ approaches.

References


Appendix A
Mislabeled Variables Task For Students

Part I.
Answer the questions on the Personal Information Survey [on next page]. Be sure to record your responses in the requested measurement units.

Part II.
Your teacher compiled the responses to the survey in a spreadsheet and then randomized the order of the columns that contained the data for questions. Thus, the columns A, B, C, … N, O, P did not match the order of the questions 1-16 on the survey. Unfortunately, he/she did this before giving each column a name for the variable that describes the measurement taken from that question.

We need to investigate this data and help the teacher label data with appropriate variable names, rather than using A, B, C…, N, O, P as variable names. In other words, which question on the survey could a set of data have come from?

Your Assignment:
You have been assigned to investigate data for two variables. Open the file containing the mislabeled survey data. For each letter variable name you are asked to investigate, think about what type of data variable is represented and use graphs to display the data. What possible questions on the survey could produce this type of data? You can use any analysis tools available to you in the software and explore any of the data from variables A-P.

For each letter variable name you were assigned, answer the following questions. Be prepared to share your answers and evidence with the class.

1. Which survey question(s) could your data match?
2. How do you know? Provide an explanation to convince another classmate.
3. How confident are you in your choice? Explain.
4. In investigating the data for this variable, did you find evidence to support a match of another variable name to any other questions? Which ones? Support your claim.
Mislabeled Variables Task
For Teachers

Part I
Have students complete the personal information survey on paper or using an online survey. Students should complete the survey a couple days prior to completing the task in class. We suggest doing the survey on a school day where the response to item 2 would reflect their typical pattern for sleep habits in preparation for school the next day. Place the survey results into a spreadsheet software and rearrange the data so it is no longer in numerical order by question number on the survey. Import the data into your favorite technology tool and name the variables with the letters A – P.

Part II
Students should work in pairs to investigate the data for two letter variables. Choose enough variables for students to explore so at least two groups are investigating the data for the same letter. This allows for different approaches and claims to emerge in the class. If a pair of students finishes early, challenge students to investigate additional data for another letter variable.

After all pairs present their finding for each letter, the class needs to come to consensus about if they are convinced by the evidence provided.

Their task is not to necessarily get the right answer, but to make a claim about the data and provide evidence to support their claim. Issues of variable types and measurements will naturally be brought to the fore as students consider the context for each question to make sense for possible values in the data.
Personal Information Survey for Students

1. How many pets do you have in your family? ____________________

2. What time did you go to bed last night? ____________________

3. How many hours of sleep did you get last night? ____________________
   (Round to nearest half hour, record with decimals such as 8.5)

4. How many letters are in your first and last name combined? ____________________

5. How many books have you read total this school year? ____________________

6. What is your gender? Answer 1 = Male and 0 = Female ____________________

7. How many siblings do you have? (include half and step) ____________________

8. How many movies did you watch in the theater last month? ____________________

9. How many times did you buy your lunch at school last week? ____________________

10. What time did you wake up on last Saturday morning? ____________________

11. How many glasses of milk do you drink daily? ____________________

12. Do you wear glasses? Answer 1 for Yes and 0 for No. ____________________

13. On what day of the month were you born? ____________________

14. How many letters are in your first name? ____________________

15. In what month were you born? ____________________
   (Answer as a number, January = 1 and December = 12)

16. What is your shoe size? ____________________
   (Use whole or half shoe sizes such as 6.5)
Appendix B
Mislabeled Variables Task For Mathematics Teacher Educators

Part I
Have students complete the personal information survey on paper or using an online survey. Students should complete the survey a couple days prior to completing the task in class. We suggest doing the survey on a school day where the response to item 2 would reflect their typical pattern for sleep habits in preparation for school the next day. Place the survey results into a spreadsheet software. If you will be using the animation after the task rearrange the data as shown below to correspond with the animation. Import the data into your favorite technology tool and name the variables with the letters A – P.

| A – #4 | E – #11 | I – #10 | M – #9 |
| B – #7 | F – #12 | J – #16 | N – #14 |
| C – #6 | G – #5  | K – #1  | O – #2 |
| D – #13| H – #8  | L – #15 | P – #3 |

Part II
Students should work in pairs to investigate the data for two letter variables. Choose enough variables for students to explore so at least two groups are investigating the data for the same letter. Make sure to assign at least two groups the following variables: C, F, I, J, O, and P. This allows for different approaches and claims to emerge in the class and for the preservice teachers to explore the same variables as in the animation. If a pair of students finishes early, challenge students to investigate additional data for another letter variable.

After all pairs present their finding for each letter, the class needs to come to consensus about if they are convinced by the evidence provided.

Their task is not to necessarily get the right answer, but to make a claim about the data and provide evidence to support their claim. Issues of variable types and measurements will naturally be brought to the fore as students consider the context for each question to make sense for possible values in the data.

Animation: https://youtu.be/fW11Ht0NPLE
Personal Information Survey for Preservice Teachers

1. How many pets do you have in your family? ____________________

2. What time did you go to bed last night? ____________________

3. How many hours of sleep did you get last night? ____________________
   (Round to nearest half hour, record with decimals such as 8.5)

4. How many letters are in your first and last name combined? ____________________

5. How many books have you read total this school year? ____________________

6. What is your gender? Answer 1 = Male and 0 = Female ____________________

7. How many siblings do you have? (include half and step) ____________________

8. How many movies did you watch in the theater last month? ____________________

9. How many times did you buy something for lunch on campus last week? ____________________

10. What time did you wake up on last Saturday morning? ____________________

11. How many glasses of milk do you drink daily? ____________________

12. Do you wear glasses? Answer 1 for Yes and 0 for No. ____________________

13. On what day of the month were you born? ____________________

14. How many letters are in your first name? ____________________

15. In what month were you born? ____________________
   (Answer as a number, January = 1 and December = 12)

16. What is your shoe size? ____________________
   (Use whole or half shoe sizes such as 6.5)